

1. 解 $y'' + 3y' + 2y = e^{-3t}$, $y(0) = 0$, $y'(0) = 2$.

$$\langle \text{解} \rangle \quad [s^2 Y(s) - sy(0) - y'(0)] + 3[sY(s) - y(0)] + 2Y(s) = \frac{1}{s+3}$$

$$[s^2 Y(s) - s \times 0 - 2] + 3[sY(s) - 0] + 2Y(s) = \frac{1}{s+3}$$

$$(s^2 + 3s + 2)Y(s) = 2 + \frac{1}{s+3}$$

$$Y(s) = \frac{2s+7}{(s+3)(s^2+3s+2)}$$

$$= \frac{2s+7}{(s+1)(s+2)(s+3)}$$

$$= \frac{A}{s+1} + \frac{B}{s+2} + \frac{C}{s+3}$$

$$= \frac{A(s+2)(s+3) + B(s+1)(s+3) + C(s+1)(s+2)}{(s+1)(s+2)(s+3)}$$

$$2s+7 = A(s+2)(s+3) + B(s+1)(s+3) + C(s+1)(s+2)$$

$$\text{令 } s = -1 \quad A(-1+2)(-1+3) = -2+7 \quad A = \frac{5}{2}$$

$$\text{令 } s = -2 \quad B(-2+1)(-2+3) = -4+7 \quad B = -3$$

$$\text{令 } s = -3 \quad C(-3+1)(-3+2) = -6+7 \quad C = \frac{1}{2}$$

$$Y(s) = \frac{5}{2} \frac{1}{s+1} - \frac{3}{s+2} + \frac{1}{2} \frac{1}{s+3}$$

$$y(t) = \frac{5}{2} e^{-t} - 3e^{-2t} + \frac{1}{2} e^{-3t}$$