

$$1. \cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 0$$

$$\cos \beta = \sqrt{1 - \cos^2 \alpha - \cos^2 \gamma} = \sqrt{1 - 0.3^2 - 0.5^2}$$

$$\cos \beta = 0.707 \quad \beta = 45^\circ$$

$$\vec{F} = 500 \times \cos 120^\circ \mathbf{i} + 500 \times \cos 45^\circ \mathbf{j} + 500 \times \cos 60^\circ \mathbf{k}$$

$$= -250 \mathbf{i} + 353.5 \mathbf{j} + 250 \mathbf{k}$$

$$2. \text{BE}(4, 3, 1) \quad U_{BE} = \frac{4}{\sqrt{39}} \mathbf{i} + \frac{3}{\sqrt{39}} \mathbf{j} + \frac{1}{\sqrt{39}} \mathbf{k}$$

$$F_x = \frac{4}{\sqrt{39}} \times 600 = 445.27 \text{ N}$$

$$F_y = \frac{3}{\sqrt{39}} \times 600 = 334 \text{ N}$$

$$F_z = \frac{1}{\sqrt{39}} \times 600 = 222.63 \text{ N}$$

$$DE = (0, 3, 0) \quad U_{DE} = \frac{0}{3} \mathbf{i} + \frac{3}{3} \mathbf{j} + \frac{0}{3} \mathbf{k}$$

$$F_{DE \parallel} = 334 \times \frac{3}{3} = 334 \text{ N}$$

$$F_{DE \perp} = \sqrt{600^2 - 334^2} = 498 \text{ N}$$